Two double-sided handwritten sheets of notes are permitted. No books or electronic aids are permitted. Please turn off your phone. There is a clock in the back of the room. Exam begins at 1:05pm and ends at 2:25pm. You have 80 minutes to earn 110 points. Good luck!
True/False with justification (3 points each)

Read each statement carefully, circle the correct answer, and write a brief justification of your answer. No points will be given if you do not provide justification.

1. **True / False** In random forest classification, one way to maximize the diversity of trees is to select at each decision node a different subset of variables during decision tree construction.

   True. As discussed in Recitation 3, at each decision node, RF choose a subset of features (usually sqrt(M)) where M is the number of total features available to the model.

2. **True / False** Increasing read length reduces the number of unresolved repetitive regions during genome assembly.

   True. Increasing read length increases the lower bound (creates a tighter lower bound) on the length of repetitive regions and increases the chance that there are reads spanning the entire repetitive region.

3. **True / False** In supervised learning, we should use all of the data available to train our model in order to generate the best model.

   False. We should keep a holdout/validation/test set in order to assess overfitting in our model.
4. **True / False** Polynomial time affine gap alignment requires more than one dynamic programming matrix.

   True. We need to keep track of the state we're in (extended/opening a gap in either sequence.)

5. **True / False** Consider the problem of identifying transcription factor motifs in a set of DNA sequences. Gibbs sampling will increase the data likelihood monotonically during its execution.

   False. Gibbs sampling is a stochastic process and does not necessarily monotonically increase data likelihood.

**Short answer (4 points each)**

6. In the Needleman-Wunsch algorithm for global alignment, what does the \((i, j)^{th}\) entry in the matrix used for dynamic programming store once it’s been filled?

   The score of a best alignment of the first \(i\) bases of the first sequence and the first \(j\) bases of the second sequences. (Also acceptable to put the recursive update formula).
7. Recall that in the BLAST algorithm, we split our query into W-mers and generate a neighborhood if these W-mers within a similarity threshold, T. Describe how the choice of \( W \) and \( T \) affects the sensitivity and specificity of the BLAST algorithm.

| Increasing W increases the specificity, decreases sensitivity. Increasing T increases sensitivity, decreases specificity |

8. In the reverse operation of the Burrows-Wheeler Transform (BWT), when obtaining the original string from the compressed string, how do you compute the second column, when you have the first and the last?

| Put the last first, then sort, and you get the second. |

9. Describe the difference between the path returned by the Viterbi algorithm and that returned by posterior decoding. What is each method maximizing?

| Viterbi gives us the most likely sequence of hidden states through our dataset, but posterior decoding gives us the most likely hidden state at each timestep, but not necessary the most likely path through them. |

Stacking interactions and pseudoknots, 3D interactions

11. Sketch the two eigenvectors that you would expect to obtain from PCA on the data in the plot above. Label the first principal component and the second principal component. Which would you expect to have the larger corresponding eigenvalue?

degree: A, betweenness and closeness: B
12. What is the source of the checkerboard/plaid pattern of genome-wide three-dimensional interactions patterns observed in high-throughput chromatin conformation capture (Hi-C) interactions?

Regions close in primary sequence tend to be nearby in 3D space. Particularly, looping structures correspond to checkerboard patterns nearby, fading out over longer distances.

13. For each of the following measures of network centrality, indicate whether node A or node B in the above figure is more central: (a) degree, (b) betweenness, and (c) closeness.

degree: A, betweenness and closeness: B
14. In eQTL discovery, what fundamental statistical problem do we overcome by only searching SNPs within a one-megabase window surrounding each target gene?

multiple hypothesis, one for every gene. mitigate by local search

15. In GWAS, why is the identification of a disease-associated region insufficient to form a therapeutic program in most cases? What are two missing pieces of information required to move forward once a disease-associated region is discovered?

Epigenomics, comparative genomics, motif match, cell type of interest, target gene, eQTL. Finding an area of the genome whose expression is correlated with a disease does not tell us anything about the biological processes that are perturbed by anomalous activity in the area that lead to a disease state. We can either adopt a bottom-up approach, where we try to find the specific pathways or processes disturbed by differential activity at each individual locus, or a top-down approach, where we consider the properties of the set of loci as a whole.

16. Why are long reads (vs. short reads) and paired-end reads (vs. single-end reads) useful in determining alternatively-spliced isoforms from RNA-seq?

The problem of determining alternatively-spliced isoforms from RNA-seq reduces to the problem of splice junction detection. Longer reads and paired-end reads increase the chance that reads span splice junctions. Paired-end reads improve the specificity of splice junction detection
17. Describe how haplotype structure (for example, blocks of linkage disequilibrium extending up to the megabase range) can both help and hinder efforts to map disease genes with large scale association studies.

Linkage disequilibrium enables us to more easily implicate a region of the genome based on the presence of disease-associated SNPs in any part of that region. However, it makes it more difficult to pinpoint the causal SNP because it isn’t immediately apparent whether a given SNP in the disease-associated region is causal or simply in linkage disequilibrium with the causal SNP.

18. What is the ‘missing heritability problem’? Describe two hypotheses put forward to explain this problem.

Single genetic variations cannot account for much of the heritability of diseases, behaviors, and other phenotypes - rare variants - common variants - wrong model assumptions

19. Recall that we can use evolutionary signatures to infer functions of the conserved regions. Describe two signatures which would characterize a protein coding region, versus two signatures which would characterize regions with important RNA structure.
20. Explain how recombination rate and time both contribute to the gradual decrease in linkage disequilibrium.
Practical Problems (20 points total)

21. You are given the following sequences and would like to determine the evolutionary relationship between them.

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<thead>
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<th>Human</th>
<th>Chimp</th>
<th>Gorilla</th>
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<td>Chimp</td>
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(a) (2 points) Using a cost of 1 for a mismatch and 0 for a match, and assuming no gaps, create a distance matrix giving the pairwise distances between each sequence.

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(b) (3 points) Is the matrix you constructed additive, ultrametric, both, or neither? Explain.

Ultrametric: for all points i, j, k − i, j, k do d(i, j) = d(i, k) = d(j, k).
Additive: for all points i, j, k, l − i, j, k, l do d(i, j) + d(k, l) = d(i, k) + d(j, l) = d(i, l) + d(j, k)

Matrix is not ultrametric: Consider H, G, C: H-G (3), H-C (1), G-C (2), two of them are not equal.

(c) (3 points) Construct a phylogenetic tree of these sequences using the UPGMA algorithm. You need not show every step.

1. H-C, node height: 1/2
2. H-C-G node height: (avg(3, 2))/2: 1.25
3. H-C-G-Z node height: avg(4, 4, 5)/2: 2.16
(d) (2 points) What does your answer to (b) tell you about the correctness of the tree that you created in (c)?

Because the matrix is not ultra metric, UPGMA is not guaranteed to produce the correct answer.
22. (5 points) You are using Gibbs sampling to discover a 5-base motif in the following five sequences:

Sequence 1: TTTTGAGTAC
Sequence 2: GCAGAATTCT
Sequence 3: ATTATTCTCG
Sequence 4: CAGATTGTGG
Sequence 5: GTTTTTTCTA

After \( t \) iterations, the maximum-score starting positions for the motif are 2,6,4,4,5 respectively for the five sequences (as underlined).

On iteration \( t + 1 \), the algorithm is going to estimate a new motif starting position for sequence 2. Calculate the motif model (in probability format) for this step. Include a pseudocount of 0.25 for all bases at all positions.

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23. (5 points) Given the following maternal and paternal genotypes and partial child genotype, impute
the missing genotypes of the child’s genotype at positions A, B, C, D. For position X, give the
possible genotypes and their frequencies. Lastly, resolve the two haplotypes of the child, except for
X.

A=0, B=0, C=1, D=0
X = 1,2 with probability 1/2 each
Haplotypes: 0010000, 01?0010
Design problem (15 points)

24. You seek to build a Hidden Markov Model (HMM) to determine which genomic locations are bound by the CTCF regulator using multiple lines of evidence.

(a) (4 points) Describe the architecture of your model. How many hidden states does your model have and what are they? What types of emission and transition probabilities? What do they represent?

(b) (3 points) List at least three data types that you expect will be informative for your problem at hand. (Hint: Not all lines of evidence need to be cell type specific.)
You now seek to extend your model to handle the same lines of evidence across multiple cell types:

(c) (2 points) What are the advantages of training a different HMM for each cell type? How would you carry out the training?

(d) (2 points) What are the advantages of training a single HMM across multiple cell types? How would you carry out the training?

(e) (4 points) Describe a learning strategy that combines advantageous features of (c) and (d).