Quiz 1
6.00 Spring 2013

Name: Very smart student
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Recitation Section:

You should complete the quiz on your own. You are allowed two sheets of notes, either handwritten or typed. You must initial every single page of the quiz!

Good luck,
6.00 staff

Question 1. (25 pts) ........___________
Question 2. (15 pts) ........___________
Question 3. (10 pts) ........___________
Question 4. (20 pts) ........___________
Question 5. (20 pts) ........___________
Question 6 (10 pts) ........___________
Question 1. (25 pts)
For each of the following blocks of code, write the output that will be printed by the code.

1.a)
```python
letters = ['a', 'b', 'c', 'd']
word = ''
for x in letters:
    word = x + word + 'x'
print word
```
Answer: `dcbaxxxx`

1.b)
```python
x = 'Global Variable'
def output(x):
    print x
output('local value')
```
Answer: `local value`

1.c)
```python
x = 'A mystery variable'
def moo(x):
    return x + ', for sure'
def foo(x):
    x = 'the other thing'
    return x
def output(x):
    x = 'or a parameter'
    x = foo('a smart choice')
    return moo(x)
print output('What will I print?')
```
Answer: `the other thing, for sure`
1.d)
def f(N):
    x = 1.0/N
    sum = 0.0
    for i in xrange(N):
        sum = sum + x;
    if sum == 1.0:
        print 'True'
    else:
        print 'False'
f(10)

Answer: False

1.e)
x = 23
y = x / 2
t = 10
t = t + 13.0
v = t / 2
print str(y) + ' and ' + str(v)

Answer: 11 and 11.5
Question 2. (15 pts)
Provide short answers to the following questions

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2.a) What number in decimal notation do the following binary mantissa and exponent represent: [111, -10]?

Answer: \(7 \times 2^2 = 1.75\)

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2.b) How do we call the following two types of knowledge (one word each):
1/ The square root of \(x\) is the number \(y\) such that \(y^2 = x\)
2/ The Newton-Raphson algorithm can compute a square root through successive approximations. At each step, the current solution is refined by solving a linearized equation based on the derivative at the current guess.

Answer:
1/ **Declarative**
2/ **Imperative**

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2.c) What does the code below compute?

```python
N=1000
NC=0.0
x=-1.0
for i in xrange(2*N):
    y=-1.0
    for j in xrange(2*N):
        if x*x+y*y<1:
            NC=NC+1
        y=y+1.0/N
    x=x+1.0/N
print NC/(N*N)
```

Answer: **Pi, or 3.1415...**
Question 3. (10 pts)
You are given a list called words with 2000 words sorted in alphabetical order. Below are three algorithms that you may use to find whether a target word is in the list.

\[
\text{def find1(words, target):}
\begin{align*}
\text{for } x \text{ in words:} & \\
& \text{if } x == \text{target:} \\
& \quad \text{return True} \\
& \text{return False}
\end{align*}
\]

\[
\text{def find2(words, target):}
\begin{align*}
& \text{size} = \text{len(words)} \\
& \text{pos} = \text{size}/2 \\
& \text{if}(\text{words[pos]} > \text{target}): \\
& \quad \text{return find2(words[0:pos], target)} \\
& \text{else:} \\
& \quad \text{return find2(words[pos:size], target)}
\end{align*}
\]

\[
\text{def find3(words, target):}
\begin{align*}
& \text{low} = 0; \\
& \text{high} = \text{len(words)} \\
& \text{while( low < high):} \\
& \quad \text{pos} = (\text{low} + \text{high})/2 \\
& \quad \text{if}(\text{words[pos]} > \text{target}): \\
& \quad \quad \text{high} = \text{pos} \\
& \quad \text{if}(\text{words[pos]} < \text{target}): \\
& \quad \quad \text{low} = \text{pos} + 1 \\
& \quad \text{if}(\text{words[pos]} == \text{target}): \\
& \quad \quad \text{return True} \\
& \text{return False}
\end{align*}
\]

3.a) One of the algorithms above is asymptotically slower, one of them is faster, and one of them is just wrong, can you tell which one is which and why (in one sentence)?

Slower: find1
Why: it is linear in the size of the words list.

Faster: find3
Why: it is doing binary search

Incorrect: find2
Why: it is recursive, but it is missing the base case. It will fail when len(words)==0
Given a polynomial represented as a list of coefficients similar to pset 2 (where the index is equal to the order, from constant to higher exponents), write a function that evaluates the polynomial for a given input number. You can assume that the list is not empty.

```python
def eval_poly(poly, x):
    """poly contains a list of floating point coefficients
    and x is a floating point number.
    Returns the value of the polynomial at x""
```

def eval_poly(poly, x):
    res = 0.0
    t = 1.0
    for u in poly:
        res = res + u * t
        t = t * x
    return res

def eval_poly(poly, x):
    res = 0.0
    t = 1.0
    for idx in xrange(len(poly)):
        u = poly[idx]
        res = res + u * t
        t = t * x
    return res
Question 5. (20 pts)

In python there are many ways of reversing a given string \( s \); for example, you can evaluate \( s[::-1] \). For this problem, you goal will be to write your own reverse function to satisfy the following requirements:

- Your function must return a new string with the same letters as the original string but in the reverse order (e.g. \( \text{reverse(‘Hello world’) must return ‘dlrow olleH’} \))
- Your function must be recursive
- Your function cannot use any built-in python mechanism that would automatically reverse the string for you (you can’t write \( s[::-1] \), for example).
- Some of the features that you can use and you will find very useful are string concatenation \( (a + b) \) and string range \( (s[a:b]) \).

```python
def reverse(myString):
    """reversal function assumes myString is a string""

    if len(myString) <= 1:
        return myString
    return reverse(myString[1:]) + myString[0]
```
Question 6 (10 pts)

Use the code below to answer the questions that follow. Note that function \( f \) assumes \( L \) has at least two elements.

```python
def f(L, x):
    """The code assumes at least 2 elements in the list L""
    def helper(L, x, low, high):
        if high-low<2:
            return low
        m=(low+high)/2
        print m # note the print
        if L[m]>x:
            return helper(L, x, low, m)
        else:
            return helper(L, x, m, high)
    return helper(L, x, 0, len(L))

L=[1, 4, 5, 6, 13]
y=f(L, 6)
print 'final value:', y
```

6.a) What does this code print (note the print statement inside the function)?

```
2
3
4
final value: 3
```

6.b) Is this algorithm iterative or recursive?

Recursive

6.c) What is the name of the algorithm?

Bisection search

6.d) What is its complexity with respect to the length \( N \) of list \( L \)?

\( O(\log(N)) \) or logarithmic

6.e) In addition to the size of the list, what key assumption does the algorithm make?

It assumes that low and high are in the range of the list.
Assumes original list is sorted.
The following questions won’t impact your grade but will help us improve the course.

How fast are the lectures? (circle one)

1. Too slow, I am bored
2. A little slow, I wish they went a little faster
3. Just right
4. A little fast, I wish they slowed down a little
5. Way too fast, If it wasn't for EdX/Office Hours/Recitations I'd be totally lost

How hard are the problem sets?

1. Too easy, I am bored
2. A little easy, I wish they were more interesting
3. Just right
4. A little hard, I wish they didn't take 10 hours to do
5. Way too hard

For each of the following, give a number from 0 to 5 based on how useful you have found it (0 is have never used it, and 5 is I couldn't live through this course without it).

1. Text Book
2. Lecture Slides
3. EdX site
4. Office Hours
5. Google